Determination of Importance Weights in QFD Using Fuzzy Analytical Hierarchical Process: Case Study

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Abstract-In the present work customer requirement is an important aspect for implementation of Quality Function Deployment (QFD) process, with the help of QFD importance weights for the customer requirements can be found out easily. For determine importance weight Analytic Hierarchy Process (AHP) has been used. For this approach customer requirement plays a vital role for forecast towards AHP. To determine the importance weights for the customer requirements fuzzy AHP approach with an extent analysis is proposed. Triangular fuzzy number used for comparison of a fuzzy AHP. For drive weight vector using the extent analysis method and their principles for comparison of fuzzy numbers. The new approach can improve the imprecise ranking of customer requirements. Prioritize customer requirements in the QFD process The fuzzy AHP with extent analysis is simple and easy to implement. For the application part the example of college to illustrate the proposed approach.


1. INTRODUCTION

Corporation’s competitiveness is directly proportional to new product development (NPD). Customer requirements would be requires for consideration for Managing NPD, competing products and technical issues. The more closely the product fits the customer’s expectations. For identifying customer needs Quality function deployment (QFD) is a well-known tool for translating customer requirements into a technical response.

For each stage of product development QFD translates customer requirements into technical specifications and production. QFD considers customer requirements by examining development space as well as product differentiation, position, and characteristics. QFD approach is appropriate for enhancement of business, R&D skills manufacturing, and management when drafting a marketing policy. QFD is based on transformation of customer needs into technical specifications.

The evaluation of (HOQ) house of quality for competitive point of view each customer requirement to combine the data of each competing product. Corporations can then employ the combined data for product differentiation and positioning. Importance ratings represent the relative importance of each customer requirement, although assigning ratings to customer requirements is sometimes made difficult by issues of objectivity and significance.

1.1. Quality Function Deployment

Quality Function Deployment (QFD) is a set of powerful product development tools that were developed in Japan to transfer the concepts of quality control from the manufacturing process into the new product development process. It is a well established, comprehensive quality system, which targets satisfaction of customer needs as a means of improving product quality. The technique identifies customer needs and translates these into technical requirements. The main features of QFD are a focus on meeting market needs by using actual customer statements (referred to as the "Voice of the Customer"), its effective application of multidisciplinary teamwork and the use of a comprehensive matrix (called the "House of Quality") for documenting information, perceptions and decisions. Some of the benefits of adopting QFD have been documented as.[1]

- Reduced time to market
- Reduction in design changes
- Decreased design and manufacturing costs
- Improved quality
- Increased customer satisfaction.

QFD utilizes "Seven Management and Planning Tools" which are used in many of its procedures:

1. Affinity diagrams.
2. Relations diagrams.
3. Hierarchy trees.
4. Matrices and tables.
5. Process Decision Program Diagrams (PDPC)
6. The Analytic Hierarchy Process (AHP)
7. Blueprinting
2. METHODOLOGY FOR RANKING IMPORTANCE OF CUSTOMER REQUIREMENT

Determining the correct importance weights for the customer requirements is essential since they significantly affect the target values set for the engineering characteristics. Various methods have been attempted to determine the importance weights. The simplest method to prioritize customer requirements is based on a point scoring scale, such as one to five or 1 to 10 (Griffin and Hauser, 1993)[13]. However, this method cannot effectively capture human perception. In order to cope with the situation in which it is difficult to isolate a set of criteria agreeable to all individuals, Ho et al. (1999)[12] developed a group decision-making technique to obtain the importance weights for the customer requirements. Gustafsson and Gustafsson (1994)[14] used a conjoint analysis method to determine the relative importance of the customer requirements. The methodology employs pairwise comparisons of the customer requirements to determine their relative importance. Yu-Chung et al.(2013)[17] introduced artificial neural networks to determine the importance weights for the customer requirements. However, the method has a strict requirement on the input variables of the neural network. With reference to the effect that the vagueness and imprecision of the importance assessment has on the customer requirements, Yu-Chung et al.(2013)[17] converted the importance assessment of the customer requirements into fuzzy numbers and then calculated the importance weights for the customer requirements using an entropy method. Vanegas and Labib (2001)[11] proposed a method to determine the weights for the customer requirements by converting the weights from the Analytic Hierarchy Process (AHP) into fuzzy numbers using the concept of a “fuzzy line segment”.

Prioritizing customer requirements can be viewed as a complex multi-criteria decision-making problem. The AHP, a multi-criteria decision-making method, has been used in weighing customer requirements [16]. The integration of the AHP into the determination of trade-off weights for the customer requirements has been proposed by Aswad (1989) and Akao (1990)[1]. Armacost et al. (1994)[15] applied the AHP to generate importance ratings for the customer requirements in a case study on industrialized housing. In the above application of the AHP to the prioritizing of customer requirements, the pairwise comparisons for each level, with respect to the goal of customer satisfaction, are conducted using a nine-point scale. The nine point scale developed by Saaty (1980)[10], expresses the preferences between the options as being either: equally, moderately, strongly, very strongly, or extremely preferred. These preferences are translated into pairwise weights of one, three, five, seven or nine, respectively, with two, four, six, eight as the intermediate values.

However, the AHP technique may suffer problems such as excessively subjective judgments, complex procedures, and being too time-consuming. Owing to the deficiencies of past techniques, this study integrates fuzzy logic into importance ranking to rank the relative importance of customer requirement and calculate the evaluating data for product positioning.[5]

2.1. AHP steps

The AHP approach, as applied to the supplier selection problem, consists of the following five steps.
1. Specify the set of criteria for evaluating the supplier’s proposals, then construct a decision hierarchy by breaking down the decision problem into a hierarchy of its elements.
2. Obtain the pair-wise comparisons of the relative importance of the criteria in achieving the goal, and compute the priorities or weights of the criteria based on this information.
3. Obtain measures that describe the extent to which each supplier achieves the criteria, then determine whether the input data satisfy a consistency test; if not, redo the pair-wise comparisons.
4. Using the information in step 3, obtain the pair-wise comparisons of the relative importance of the suppliers with respect to the criteria, and compute the corresponding priorities.
5. Using the results of steps 2 and 4, a final priority vector of each supplier is obtained by synthesizing all the priority vectors to achieve the goal of the hierarchy.

3. FUZZY AHP

There is an extensive literature that addresses the situation where the comparison ratios are imprecise judgments (Leung ve Chao, 2000). In most of the real-world problems, some of the decision data can be precisely assessed while others cannot. Humans are unsuccessful in making quantitative predictions, whereas they are comparatively efficient in qualitative forecasting (Kulak ve Kahraman, 2005). Essentially, the uncertainty in the preference judgments give rise to uncertainty in the ranking of alternatives as well as difficulty in determining consistency of preferences (Leung ve Chao, 2000). These applications are performed with many different perspectives and proposed methods for fuzzy AHP.[18]

Fuzzy AHP steps

Some calculation steps are essential and explained as follows:
1. Establishing the hierarchical structure Constructing the hierarchical structure with decision elements, decision-makers are requested to make pairwise comparisons between decision alternatives and criteria using a nine-point scale. All matrices are developed
and all pair-wise comparisons are obtained from each 
n decision-maker(s).
2. Calculating the consistency to ensure that the 
priority of elements is consistent, the maximum 
eigenvector or relative weights and max λ is 
calculated. Then, the consistency index (CI) for each 
matrix order n is computed by using Eq. (1).

Based on the CI and random index (RI), the 
consistency ratio (CR) is calculated using Eq. (2). The 
CI and CR are defined as follows (Saaty, 1980):

\[ C.I = (\lambda_{max} - n) / (n-1) \] .............................. (1)

\[ C.R = C.I / R.I \] .......................... (2)

where, n is the number of items being compared in the matrix, max λ is the largest eigenvalue and RI is a random consistency index obtained from a large number of simulation runs and varies upon the order of matrix (see Table 1).

<table>
<thead>
<tr>
<th>N</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>RI</td>
<td>0</td>
<td>0</td>
<td>0.58</td>
<td>0.90</td>
<td>1.12</td>
<td>1.24</td>
<td>1.32</td>
<td>1.41</td>
</tr>
<tr>
<td>N</td>
<td>8</td>
<td>9</td>
<td>10</td>
<td>11</td>
<td>12</td>
<td>13</td>
<td>14</td>
<td>15</td>
</tr>
<tr>
<td>RI</td>
<td>1.41</td>
<td>1.45</td>
<td>1.49</td>
<td>1.51</td>
<td>1.48</td>
<td>1.56</td>
<td>1.57</td>
<td>1.58</td>
</tr>
</tbody>
</table>

3. Constructing a fuzzy positive matrix A decision-maker transforms the score of pair-wise comparison into linguistic variables via the positive triangular fuzzy number (PTFN). The fuzzy positive reciprocal matrix can be defined as

\[ A^{k} = [A_{ij}^{k}] \]

where, \( A^{k} \) is a fuzzy position reciprocal matrix of decision-maker \( k \); \( A_{ij}^{k} \) is the relative importance between \( i \) and \( j \) of decision elements[19]

\[ \tilde{A}_{ij}^{k} = 1, \quad \forall i = j \], \quad \tilde{A}_{ij}^{k} = 1 / \tilde{A}_{ji}^{k}, \quad \forall i, j = 1, 2, ..., n 

Calculating fuzzy weights value

According to the Lambda-Max method proposed by 
Csutora and Buckley (2001), the fuzzy weights of the hierarchy can be calculated. This process is described as follows:

Let \( \alpha = 1 \) to obtain the positive matrix of 
decision-maker. \( \tilde{A}_{m}^{k} = [a_{ij}]_{m \times n} \). Then, apply the 
AHP to calculate weight matrix \( \tilde{w}_{m}^{k} \)

\[ w_{m}^{k} = [\tilde{w}_{m}^{k}]_{i = 1, 2, ..., n} \]

Let \( \alpha = 0 \) to obtain the lower bound and upper bound of 
the positive matrix of decision-maker, \( \tilde{A}_{m}^{k} = [a_{ij}]_{m \times n} \) and \( \tilde{A}_{m}^{k} = [a_{ij}]_{m \times n} \). Then, apply the 
AHP to calculate the weight matrix: \( \tilde{w}_{m}^{k} \) and \( \tilde{w}_{m}^{k} \)

\[ w_{m}^{k} = [\tilde{w}_{m}^{k}]_{i = 1, 2, ..., n} \]

\[ w_{m}^{k} = [\tilde{w}_{m}^{k}]_{i = 1, 2, ..., n} \]

- To ensure the fuzziness of weight, two constants, i.e \( S_{l}^{k} \) and \( S_{u}^{k} \), are calculated as follows:

\[ S_{l}^{k} = \min \{ w_{mi} / w_{bj} \} \quad 1 \leq i \leq n \]

\[ S_{u}^{k} = \min \{ w_{mi} / w_{bj} \} \quad 1 \leq i \leq n \]

The lower bound \( W_{l}^{k} \) and upper bound \( W_{u}^{k} \) of the weight matrix are defined as:

\[ W_{l}^{k} = [W_{il}^{k}], \quad W_{u}^{k} = S_{l}^{k} W_{il}^{k}, \quad i = 1, 2, ..., n \]

\[ W_{u}^{k} = [W_{iu}^{k}], \quad W_{u}^{k} = S_{u}^{k} W_{iu}^{k}, \quad i = 1, 2, ..., n \]

- Aggregating \( W_{l}^{k} \), \( W_{u}^{k} \), and \( W_{u}^{k} \), the fuzzy weight for decision-maker \( k \) can be acquired as follows:

\[ \tilde{w}_{i}^{k} = (w_{i}^{k}, w_{i}^{k}, w_{i}^{k}) \]

\[ w_{i}^{k} = \frac{1}{k} \left( \tilde{w}_{i}^{1} \otimes \tilde{w}_{i}^{2} \otimes \cdots \otimes \tilde{w}_{i}^{n} \right) \]

where,

\[ \tilde{w}_{i}^{k} : \text{The fuzzy weight of decision-makers } i \text{ is incorporated with } K \text{ decision-makers.} \]

\[ \tilde{w}_{i}^{k} : \text{The fuzzy weight of decision element } i \text{ of } K \text{ decision-maker.} \]

\( k \): number of decision-makers.

4. THE PRINCIPLES FOR COMPARISON 
OF MATRIX

The principles for the comparison of fuzzy numbers were introduced to derive the weight vectors of all elements for each level of the hierarchy with the use of fuzzy synthetic values. We now discuss these principles that allow the comparison of fuzzy numbers

[6] [7] [8]

Definition 1. M1 and M2 are two triangular fuzzy numbers. The degree of possibility of \( M1 \) \( \geq M2 \) is defined as \( V(M1 \geq M2) = \sup x \\leq y \left[ \min (\mu M1(x), \mu M2(y)) \right] \)

Theorem 1. If \( M1 \) and \( M2 \) are triangular fuzzy numbers that are denoted by \( (11, m1, u1) \) and \( (12, m2, u2) \) respectively, then:

1. The necessary and sufficient condition of \( V(M1 \geq M2) = 1 \) is \( m1 \geq m2 \).

2. If \( m1 \leq m2 \), then

\[ V(M1 \geq M2) = (12-u1)/(11-u1)-(m2-l2), \quad l2 \leq u1 \]
\[ = 0 , \]

otherwise

**Definition 2.** The degree of possibility for a fuzzy number to be greater than \( k \) fuzzy numbers \( M_i \) \((i=1,2,\ldots,k)\) can be defined by

\[ \text{V}(M \geq M_1,M_2,\ldots,M_k)=\min V (M \geq M_i) \]

Let \( d(p) = \min V (S \geq S_j) \), where, \( p \) is the \( j \)th element of the \( k \)th level, \( j = 1, 2, \ldots, n \). The number of elements in the \( k \)th level is \( n \).

Then the weight vector of \( k \)th level is obtained as:

\[ w_k^k = (d(p_1) \cdot d(p_2) \ldots \ldots d(p_k))^T \]

After normalization, the normalized weight vector, \( W \), is:

\[ \begin{bmatrix} w_k^k \end{bmatrix} = \begin{bmatrix} w_1^k \cr w_2^k \cr \vdots \cr w_n^k \end{bmatrix} \]

\[ \begin{bmatrix} w_k \end{bmatrix} \]

**5. WORK IMPLEMENTATION**

Present work has been considering the case of college as case study. The objective of this case study using Fuzzy AHP for prioritizing the student’s requirements is the progress of the college. Now we are applying the Fuzzy AHP step by step to evaluate the student’s requirements and achieving the goal of progress of the college.

**5.1. Hierarchical Structure**

![Hierarchical structure for the case of college](image)

To obtain the students requirements for the progress of college, two different types are considered: girls and boys. Discussions with these two groups reveal a total of 8 requirements for the progress of college. All the requirements are categorized with use of an affinity diagram. Figure 1 shows a three level hierarchy for the students requirements for progress of college. In fig 1. the goal is “progress of college”.

**5.2. Construction of fuzzy judgment matrix**

The participants in the focus group use the Fuzzy AHP scale to express their preferences between options. Then pair wise comparison matrix is obtained for each hierarchical level as follows:

Table 2. FAHP Scales

<table>
<thead>
<tr>
<th>Definition</th>
<th>Intensity of Performance</th>
</tr>
</thead>
<tbody>
<tr>
<td>EQUAL</td>
<td>(1,1,1)</td>
</tr>
<tr>
<td>WEAK</td>
<td>(2/3,1,3/2)</td>
</tr>
<tr>
<td>FAIRLY STRONG</td>
<td>(3/2,2,5/2)</td>
</tr>
<tr>
<td>VERY STRONG</td>
<td>(5/2,3,7/2)</td>
</tr>
<tr>
<td>ABSOLUTE</td>
<td>(7/2,4,9/2)</td>
</tr>
</tbody>
</table>

Fuzzy judgment matrix:
Consistency index & consistency ratio
CI = (λ_{max} – n)/(n-1),
CR = (CI / RI(n))100%,
Acceptable consistency of a pairwise judgment:
if calculated CR<10%

5.3. Determination Of Fuzzy Synthetic Degree Values

The fuzzy synthetic degree values of all elements for the category and sub-category level of the hierarchy can be calculated as shown below:

\[ \sum \sum a_{ij} = (1, 1, 1) + (2, 2.5, 3) + \ldots + (1, 1, 1) \]
\[ = (9.43, 11.23, 13.4) \]

\[ \left( \sum \sum a_{ij} \right) = (0.075, 0.089, 0.106) \]
\[ \sum a_{ij} = (1, 1, 1) + (2, 2.5, 3) + (2.5, 3, 3.5) \]
\[ = (5.5, 6.5, 7.5) \]

Hence, the fuzzy synthetic degree values of the element C1, DC1, can be calculated as follows:

\[ DC1 = \sum a_{1j} \times \left( \sum \sum a_{ij} \right) \]
\[ = (5.5, 6.5, 7.5) \times (0.075, 0.089, 0.106) \]
\[ = (0.41, 0.58, 0.79) \]

Following a similar calculation, the fuzzy synthetic degree values of all elements of the hierarchy level can be obtained as shown below:

\[ DC1 = (0.41, 0.58, 0.79), DC2 = (0.15, 0.21, 0.32), DC3 = (0.15, 0.21, 0.32) \]
\[ DS1 = (0.11, 0.13, 0.17), DS2 = (0.41, 0.55, 0.74), DS3 = (0.23, 0.31, 0.41), DS4 = (0.24, 0.29, 0.35), DS5 = (0.54, 0.71, 0.92) \]
\[ DS6 = (0.36, 0.49, 0.66), DS7 = (0.29, 0.37, 0.48), DS8 = (0.10, 0.12, 0.15) \]

5.4 Calculation of weight vectors

Fuzzy numbers are compared, on the basis of principals discussed earlier, to derive the weight vectors of all elements for each level of the hierarchy with the use of fuzzy synthetic degree values.

\[ V(DC1 \geq DC2) = 1, V(DC1 \geq DC3) = 1, V(DC2 \geq DC1) = 0, V(DC2 \geq DC3) = 1, V(DC3 \geq DC1) = 0, V(DC3 \geq DC2) = 1 \]
\[ d(C1) = \min V(DC1 \geq DC2, DC3) \]
\[ = \min \{1, 1\} = 1 \]

\[ d(C2) = \min V(DC2 \geq DC1, DC3) \]
\[ = \min \{0, 1\} = 0 \]
\[ d(C3) = \min V(DC3 \geq DC1, DC2) \]
\[ = \min \{0, 1\} = 0 \]

\[ WG = (d(C1), d(C2), d(C3)) = (1.00, 0.00, 0.00) \]

The normalized weight vectors of the category level:

\[ G: (WC1, WC2, WC3) = (1.00, 0.00, 0.00) \]
\[ V(DS1 \geq DS2) = 0 \]
\[ V(DS1 \geq DS3) = 0 \]
\[ V(DS2 \geq DS1) = 1 \]
\[ V(DS2 \geq DS3) = 1 \]
\[ V(DS3 \geq DS1) = 1 \]
\[ V(DS3 \geq DS2) = 0 \]
\[ d(S1) = 0, d(S2) = 1, d(S3) = 0 \]

Normalized wt. vectors = (0.00, 1.00, 0.00)

\[ V(DS4 \geq DS5) = 0 \]
\[ V(DS5 \geq DS4) = 1 \]
\[ d(S4) = 0, d(S5) = 1 \]

Normalized wt. vectors = (0.00, 1.00)

\[ V(DS6 \geq DS7) = 1 \]
\[ V(DS6 \geq DS8) = 1 \]
\[ V(DS7 \geq DS6) = 0.360.5 \]
\[ V(DS7 \geq DS8) = 1 \]
\[ V(DS8 \geq DS6) = 0 \]
\[ V(DS8 \geq DS7) = 0 \]
\[ d(S6, S7, S8) = (1, 0.5, 0) \]

Normalized wt. vectors = (0.67, 0.33, 0.00)

TABLE 3: Importance weights for the students requirements for the progress of the college

<table>
<thead>
<tr>
<th>CATEGORY</th>
<th>SUBCATEGORY</th>
</tr>
</thead>
<tbody>
<tr>
<td>Education (1.00)</td>
<td>TRAINING PROGRAMS &amp; INDUSTRIAL TOURS (0.00)</td>
</tr>
<tr>
<td></td>
<td>PLACEMENT (1.00)</td>
</tr>
<tr>
<td></td>
<td>INTERNET &amp; LIBRARY FACULTY (0.00)</td>
</tr>
<tr>
<td>EXTRA-CURRICULAR ACTIVITIES (0.00)</td>
<td>RECRATIONAL ACTIVITIES (0.00)</td>
</tr>
<tr>
<td>INFRASTRUCTURE (0.00)</td>
<td>TECHNICAL &amp; CULTURAL ACTIVITIES (1.00)</td>
</tr>
<tr>
<td>CIVIL AMENITIES (0.07)</td>
<td>HOSPITAL &amp; BANKING FACILITIES (0.33)</td>
</tr>
<tr>
<td></td>
<td>CONSTRUCTION (0.00)</td>
</tr>
</tbody>
</table>
6. CONCLUSION

For product planning Determining the relative importance of customer requirements is a fundamental problem in QFD. So address this problem The AHP has been widely used. However, the use of a discrete scale of one to nine in the conventional AHP has the disadvantage that it cannot take into account the uncertainty and ambiguity inherent in the assessment of customer requirements. In fact, for the customer requirements determining the relative importance involves a high degree of subjective judgment and individual preference. In this work, a Fuzzy AHP with extent analysis has been described to determine the importance weights for the customer requirements for QFD. To calculate the importance weights for the customer requirements the fuzzy AHP with extent analysis is an effective method due to capability of human judgement. So the algorithm for fuzzy AHP makes it simple to determine the weight vectors and it is easy to implement with extent analysis. So it is analysed that calculation of eigenvectors required by the conventional AHP is no longer necessary. A example of college is used to illustrate the application of the approach. According to this study the normalized vector (0.67, 0.33, 0.00) have been lies in between 0 to 1 that is the requirement for the progress of college .so it has been clear that the condition having followed by the normalized vector so the direction towards progress of college is appropriate.

REFERENCES

[13] Griffin et al., voice of the customer, wiem05-020 elements supplied: 1,2,3,4,5,6,8,10
[14] Gustafsson et al., 1989; Gustafsson & Wigstrom
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